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## Cloud: Security risks in public-key cryptography

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# Cloud: Security risks in public-key cryptography

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### **Abstract**

This deliverable serves as a progress report on Task 3.2 (“share files”) of the work package 3 (“Post-quantum cryptography for the cloud”) of the PQCRYPTO project. The main purpose of this task is to identify some of the most promising techniques for public key cryptography for long term security in particular against a quantum adversary. The current document will present some preliminary results, mostly on the cryptographic techniques we wish to promote, and raise some issue concerning their security.

**Keywords:** public key cryptography, post-quantum, code-based, hash-based, lattice-based , multivariate



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## 1 Introduction

The main objectives of WorkPackage 3 is to understand the means to provide very long term (50 years) protection for users data in the cloud. The Task 3.2 is dedicated to public-key cryptography, namely public-key digital signatures and public-key encryption and key exchange mechanisms.

The present deliverable makes a first assessment of the situation, reports the findings of the project participants, and raises some issues to be explored within the project lifetime and beyond. The task is focused on two target systems, hash-based digital signatures and the McEliece public-key encryption scheme. However, beyond that, the project and its participants are concerned with any research, applied and fundamental, aiming at a better understanding and a better design of cryptographic solutions for long term security, in particular in the presence of an adversary endowed with quantum computing capabilities.

During the 18 months of the reported period and within the scope of the task 3.2, the participants of the PQCRIPTO project have produced 16 research publications which have appeared in relevant international conferences and journals. In addition, they have produced 10 preprints. This preliminary report categorizes those works and explains how they coherently aggregate towards the project goals.

## 2 Digital Signature

### 2.1 Hash-Based Signatures

In the area of hash-based signatures, the participants produced several important results during the first 18 project months. Project members were and are involved in the ongoing standardization of XMSS, a stateful hash-based signature scheme, within IRTF [HBGM15], the analysis of the security of hash-based signatures [HRS16b], research on the feasibility of implementations (of hash-based signatures) on resource-constrained devices [HRS16a], and the construction of short, fixed-length input hash functions [KLMR16, GM16].

Project members are authoring an Internet-Draft within the *crypto forum research group* (CFRG) of the *Internet research task force* (IRTF). The draft is currently in last call and awaits a document shepherd for publication as *request for comments* (RFC). Besides authoring the Internet Draft, project members presented a tightened security reduction for the scheme described in the draft [HRS16b]. Compared to previous versions of the scheme, this tightened security analysis justifies to select shorter hash function output lengths, reducing the signature size, while preserving the security level. It also justifies to use a 256-bit hash function for the 256-bit classical and 128-bit quantum security level. The results can also be applied to the stateless hash-based signature scheme SPHINCS, proposed by several project members [BHH<sup>+</sup>15].

In the same work [HRS16b], project members present lower bounds on the complexity of generic quantum attacks against the security properties of hash functions underlying XMSS. This was the first work formally justifying post-quantum security claims of XMSS, as long as a hash function is used that does not have specific quantum weaknesses. The latter is assumed to apply to all “engineered” hash functions like SHA2, or SHA3.

The only practical proposal for stateless hash-based signatures so far is SPHINCS. While it achieves reasonable speed on standard CPUs (14ms on Intel Haswell CPUs) and also signature sizes reasonable on normal platforms (41KB), speed and sizes might become an issue on

resource-constrained devices. To evaluate the feasibility of using SPHINCS on such resource-constrained devices, project members did an implementation [HRS16a] on an ARM Cortex M3 with only 16KB working memory<sup>1</sup>. Although it was possible to demonstrate feasibility, the results also show that, on such constrained devices, a lot of struggle can be avoided if the specific setting permits the use of stateful hash-based signature schemes.

The hash-functions used within hash-based signature schemes map short, fixed-length inputs to short outputs. This is not the typical setting today’s hash functions are designed for and they often achieve good performance only for long variable-length inputs. Hence, the performance of hash based signatures can be improved constructing dedicated hash functions for the short, fixed-length input setting. Project members proposed two such dedicated hash functions: Haraka [KLMR16] and Simpira [GM16]. The first benchmarks for SPHINCS using Haraka suggest that one can expect a speed-up of factor 1.99/1.87/2.86 for key generation/signing/verification on Intel Skylake CPUs.

Both Haraka and Simpira utilize AES-NI and are therefore limited to standard CPUs on newer platforms. However, recent ARM platforms (ARMv8) also come with AES specific instructions which might also allow a very efficient implementation. This aspects needs to be evaluated for both candidates. For more constrained devices it could still be interesting to explore other design strategies, if the main limiting factor are not the memory requirements.

## 2.2 Other Signatures

In complement to our efforts to improve and promote hash-based signatures, we had several contributions, one for lattice-based signatures [ABB<sup>+</sup>16] and one for multivariate signatures [PCY<sup>+</sup>15].

In addition, we are exploring other promising directions, namely digital signature schemes based on Zero-Knowledge (ZK) protocols. Since Fiat and Shamir seminal work [FS87], ZK protocols can be transformed into signature scheme. The so-called Non-Interactive Zero-Knowledge (NIZK) protocols can be derived from various quantum resistant primitives, in particular from multivariate crypto [CHR<sup>+</sup>16] and code-based crypto [Sen16], but also lattice-based crypto. Those construction have some merits but they have security issues which are discussed in §5.

## 3 Public-Key Encryption / Key Exchange Mechanisms

### 3.1 McEliece Encryption Scheme

The original McEliece public-key encryption scheme, using binary Goppa codes, has successfully resisted to almost 40 years of cryptanalysis efforts. It enjoys numerous interesting features: its security is well understood and can be accurately estimated in the current state of the art and it can be efficiently and securely implemented [BCS13]<sup>2</sup>. This system can be considered as mature and, during this eighteen months period, no researcher within the project or outside has found results changing the state of the art.

One limitation of the scheme comes from the size of the public keys, which make it less suitable for some applications, as key exchange mechanisms with forward secrecy in which a public key has to be transmitted at every instance of the scheme. To improve this aspect

<sup>1</sup>This work was performed within WP1, we mention it here for the sake of completeness

<sup>2</sup><http://www.win.tue.nl/~tchou/mcbits/>

a quasi-cyclic variant, namely QC-MDPC-McEliece has been proposed recently [MTSB13], with similarly good security arguments and an easy implementation [HvMG13, Cho16]. A very recent result<sup>3</sup> points out the existence of decryption failure and how to use them to recover the secret key. This side channel attack do not threaten all applications, in particular key exchange mechanisms can avoid it. However, this issue must be addressed and the design failure-free variants of QC-MDPC-McEliece is one of the challenges that the project participants intend to solve. A first step has already been made [CS16].

### 3.2 Other techniques

Multivariate crypto also offers some interesting lines of work to produce really public-key encryption schemes [SDP15].

Last but not least, in the first 18 months of the project, some of our contributions to produce key exchange mechanisms based on lattices have recieved at lot of attention [ADPS16, BCD<sup>+</sup>16b] and is likely to produce secure and practical primitives. We definitely intend to pursue this research direction.

## 4 Security Assessment

### 4.1 Generic Techniques

This category of security arguments relates to the underlying hard algorithmic problems. Those problems are essentially, finding short vectors (lattice-based crypto), decoding in a linear code (code-based crypto), or solving polynomial systems (multivariate crypto). They are of major importance for selecting secure parameters for the considered schemes. The key issues are to keep track and to contribute to the state of the art for the design of algorithms solving those problems, and, in the case of this project, to find their best quantum variants.

The participants have contributed in lattice-based cryptography with two papers, the first improves the state of the art for computing short vectors in ideal lattices [BNvdP16], the second proves that instances of LWE with binary errors can be solved more efficiently than expected [BGPW16].

We also have two results for code-based cryptography, the first one explores the case where the error weight is small compared with the code length and concludes that all recent improvements of generic decoding techniques are inefficient in that case [CTS16]. This is important in practice since the QC-MDPC-McEliece variant falls into this category. Another work deals with generic decoding for the rank metric [HT15]. Rank metric is an alternative to the Hamming metric for designing code-based cryptosystems, the research community needs to explore the possibilities and limitations of this technique.

### 4.2 Structural Attacks

This second category of security arguments relates to attacks or properties which target a specific variant of the schemes.

Two of our contributions relate to lattices, more specifically to Ring-LWE, and expose weaknesses of particular variants [CIV16b, CIV16a].

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<sup>3</sup>Thomas Johansson, Paul Stankovski and Qian Guo, *A Key Recovery Attack on MDPC with CCA Security Using Decoding Errors*, to appear at ASIACRYPT, in December 2016

Two other contributions prove that some specific constructions of code-based cryptography are unsafe, one breaks a variant of McEliece using polar codes [BCD<sup>+</sup>16a] and the other breaks a digital signature scheme based on LDGM (Low Density Generator Matrix) codes [PT16].

Other results [FOP<sup>+</sup>16b, FOP<sup>+</sup>16a, CCP14] relate to code-based cryptography, and though they do not break a specific proposed scheme, they help to understand the limits of what is secure and what is not when designing code-based public-key schemes.

## 5 Some Issues with Protocols in a Quantum Setting

The Fiat-Shamir construction [FS87] is a way to transform a zero-knowledge protocol into a signature scheme. Even if the underlying computational assumptions are secure against quantum adversaries, the security proof itself doesn't directly imply security against quantum adversaries. Some proof techniques, such as *rewinding* or the use of a *random oracle*, do not translate immediately to the quantum setting and require more work.

**Quantum rewinding.** When considering for example zero-knowledge protocols, we need to construct an efficient simulator that will simulate the distribution of transcripts between the prover and the verifier. In order to do so, we often ask this simulator to perform backtracking also called in this setting rewinding. Some outcomes of the simulator will be invalid transcripts and we ask the simulator to go back to a previous step of the simulation and start again with new randomness. In the quantum setting, we would also ask the quantum simulator to rewind to a previous state in the computation. This rewinding can depend on some outcomes *i.e.* measurements of the simulator and therefore its reversibility is lost. An additional complication is that the simulator has access to a single copy of prior knowledge, an auxiliary quantum state, that he uses for the simulation so this quantum rewinding should not destroy this state.

**Quantum random oracle model** In the random oracle model, hash functions used in some cryptographic protocol are replaced by idealized random functions, which sometimes helps in proving security of the protocol. In order to prove security, it is often required to tweak the random oracle depending on past inputs. In the quantum setting, queries to the random oracle can be made in superposition. When the input of the random oracle is not a well defined string, those tweaking techniques do not necessarily apply and therefore proving security is more challenging and requires techniques tailored for this quantum setting.

In [Unr15], Unruh showed how solve these problems specifically for the Fiat Shamir construction. However several other constructions are still not known to be secure against quantum adversaries.

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